

1. Find the *names* of suppliers who supply some red part.
2. Find the *sids* of suppliers who supply some red or green part.
3. Find the *sids* of suppliers who supply some red part or are at 221 Packer Ave.
4. Find the *sids* of suppliers who supply some red part and some green part.
5. Find the *sids* of suppliers who supply every part.
6. Find the *sids* of suppliers who supply every red part.
7. Find the *sids* of suppliers who supply every red or green part.
8. Find the *sids* of suppliers who supply every red part or supply every green part.
9. Find pairs of *sids* such that the supplier with the first *sid* charges more for some part than the supplier with the second *sid*.
10. Find the *pids* of parts that are supplied by at least two different suppliers.
11. Find the *pids* of the most expensive parts supplied by suppliers named Yosemite Sham.
12. Find the *pids* of parts supplied by every supplier at less than \$200. (If any supplier either does not supply the part or charges more than \$200 for it, the part is not selected.)

**Answer 4.3** In the answers below RA refers to Relational Algebra, TRC refers to Tuple Relational Calculus and DRC refers to Domain Relational Calculus.

1. ■ RA

$$\pi_{sname}(\pi_{sid}((\pi_{pid}\sigma_{color='red'}Parts) \bowtie Catalog) \bowtie Suppliers)$$

- TRC

$$\{T \mid \exists T1 \in Suppliers(\exists X \in Parts(X.color = 'red' \wedge \exists Y \in Catalog (Y.pid = X.pid \wedge Y.sid = T1.sid)) \wedge T.sname = T1.sname)\}$$

- DRC

$$\{\langle Y \rangle \mid \langle X, Y, Z \rangle \in Suppliers \wedge \exists P, Q, R(\langle P, Q, R \rangle \in Parts \wedge R = 'red' \wedge \exists I, J, K(\langle I, J, K \rangle \in Catalog \wedge J = P \wedge I = X))\}$$

- SQL

```

SELECT S.sname
FROM   Suppliers S, Parts P, Catalog C
WHERE  P.color='red' AND C.pid=P.pid AND C.sid=S.sid
    
```

2. ■ RA

$$\pi_{sid}(\pi_{pid}(\sigma_{color='red' \vee color='green'} Parts) \bowtie catalog)$$

■ TRC

$$\{T \mid \exists T1 \in Catalog(\exists X \in Parts((X.color = 'red' \vee X.color = 'green') \wedge X.pid = T1.pid) \wedge T.sid = T1.sid)\}$$

■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists A, B, C(\langle A, B, C \rangle \in Parts \wedge (C = 'red' \vee C = 'green') \wedge A = Y)\}$$

■ SQL

```

SELECT C.sid
FROM   Catalog C, Parts P
WHERE  (P.color = 'red' OR P.color = 'green')
AND    P.pid = C.pid
    
```

3. ■ RA

$$\begin{aligned} & \rho(R1, \pi_{sid}((\pi_{pid} \sigma_{color='red'} Parts) \bowtie Catalog)) \\ & \rho(R2, \pi_{sid} \sigma_{address='221PackerStreet'} Suppliers) \\ & R1 \cup R2 \end{aligned}$$

■ TRC

$$\begin{aligned} & \{T \mid \exists T1 \in Catalog(\exists X \in Parts(X.color = 'red' \wedge X.pid = T1.pid) \\ & \wedge T.sid = T1.sid) \\ & \vee \exists T2 \in Suppliers(T2.address = '221PackerStreet' \wedge T.sid = T2.sid)\} \end{aligned}$$

■ DRC

$$\begin{aligned} & \{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists A, B, C(\langle A, B, C \rangle \in Parts \\ & \wedge C = 'red' \wedge A = Y) \\ & \vee \exists P, Q(\langle X, P, Q \rangle \in Suppliers \wedge Q = '221PackerStreet')\} \end{aligned}$$

■ SQL

```

SELECT S.sid
FROM   Suppliers S
WHERE  S.address = '221 Packer street'
      OR S.sid IN ( SELECT C.sid
                   FROM   Parts P, Catalog C
                   WHERE  P.color='red' AND P.pid = C.pid )

```

## 4. ■ RA

$$\rho(R1, \pi_{sid}((\pi_{pid} \sigma_{color='red'} Parts) \bowtie Catalog))$$

$$\rho(R2, \pi_{sid}((\pi_{pid} \sigma_{color='green'} Parts) \bowtie Catalog))$$

$$R1 \cap R2$$

## ■ TRC

$$\{T \mid \exists T1 \in Catalog (\exists X \in Parts (X.color = 'red' \wedge X.pid = T1.pid) \\ \wedge \exists T2 \in Catalog (\exists Y \in Parts (Y.color = 'green' \wedge Y.pid = T2.pid) \\ \wedge T2.sid = T1.sid) \wedge T.sid = T1.sid)\}$$

## ■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists A, B, C (\langle A, B, C \rangle \in Parts \\ \wedge C = 'red' \wedge A = Y) \\ \wedge \exists P, Q, R (\langle P, Q, R \rangle \in Catalog \wedge \exists E, F, G (\langle E, F, G \rangle \in Parts \\ \wedge G = 'green' \wedge E = Q) \wedge P = X)\}$$

## ■ SQL

```

SELECT C.sid
FROM   Parts P, Catalog C
WHERE  P.color = 'red' AND P.pid = C.pid
      AND EXISTS ( SELECT P2.pid
                  FROM   Parts P2, Catalog C2
                  WHERE  P2.color = 'green' AND C2.sid = C.sid
                  AND P2.pid = C2.pid )

```

## 5. ■ RA

$$(\pi_{sid, pid} Catalog) / (\pi_{pid} Parts)$$

## ■ TRC

$$\{T \mid \exists T1 \in Catalog (\forall X \in Parts (\exists T2 \in Catalog \\ (T2.pid = X.pid \wedge T2.sid = T1.sid)) \wedge T.sid = T1.sid)\}$$

■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \forall \langle A, B, C \rangle \in Parts \\ (\exists \langle P, Q, R \rangle \in Catalog (Q = A \wedge P = X))\}$$

■ SQL

```
SELECT C.sid
FROM   Catalog C
WHERE  NOT EXISTS (SELECT P.pid
                   FROM   Parts P
                   WHERE  NOT EXISTS (SELECT C1.sid
                                     FROM   Catalog C1
                                     WHERE  C1.sid = C.sid
                                     AND   C1.pid = P.pid))
```

6. ■ RA

$$(\pi_{sid, pid} Catalog) / (\pi_{pid} \sigma_{color='red'} Parts)$$

■ TRC

$$\{T \mid \exists T1 \in Catalog (\forall X \in Parts (X.color \neq 'red' \\ \vee \exists T2 \in Catalog (T2.pid = X.pid \wedge T2.sid = T1.sid)) \\ \wedge T.sid = T1.sid)\}$$

■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \forall \langle A, B, C \rangle \in Parts \\ (C \neq 'red' \vee \exists \langle P, Q, R \rangle \in Catalog (Q = A \wedge P = X))\}$$

■ SQL

```
SELECT C.sid
FROM   Catalog C
WHERE  NOT EXISTS (SELECT P.pid
                   FROM   Parts P
                   WHERE  P.color = 'red'
                   AND   (NOT EXISTS (SELECT C1.sid
                                     FROM   Catalog C1
                                     WHERE  C1.sid = C.sid AND
                                     C1.pid = P.pid)))
```

7. ■ RA

$$(\pi_{sid, pid} Catalog) / (\pi_{pid} \sigma_{color='red' \vee color='green'} Parts)$$

- TRC

$$\{T \mid \exists T1 \in Catalog(\forall X \in Parts((X.color \neq 'red' \wedge X.color \neq 'green') \vee \exists T2 \in Catalog(T2.pid = X.pid \wedge T2.sid = T1.sid)) \wedge T.sid = T1.sid)\}$$

- DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \forall \langle A, B, C \rangle \in Parts((C \neq 'red' \wedge C \neq 'green') \vee \exists \langle P, Q, R \rangle \in Catalog(Q = A \wedge P = X))\}$$

- SQL

```
SELECT C.sid
FROM   Catalog C
WHERE  NOT EXISTS (SELECT P.pid
                   FROM   Parts P
                   WHERE  (P.color = 'red' OR P.color = 'green')
                   AND   (NOT EXISTS (SELECT C1.sid
                                     FROM   Catalog C1
                                     WHERE  C1.sid = C.sid AND
                                             C1.pid = P.pid)))
```

8. ■ RA

$$\begin{aligned} & \rho(R1, ((\pi_{sid, pid} Catalog) / (\pi_{pid} \sigma_{color='red'} Parts))) \\ & \rho(R2, ((\pi_{sid, pid} Catalog) / (\pi_{pid} \sigma_{color='green'} Parts))) \\ & R1 \cup R2 \end{aligned}$$

- TRC

$$\{T \mid \exists T1 \in Catalog((\forall X \in Parts(X.color \neq 'red' \vee \exists Y \in Catalog(Y.pid = X.pid \wedge Y.sid = T1.sid)) \vee \forall Z \in Parts(Z.color \neq 'green' \vee \exists P \in Catalog(P.pid = Z.pid \wedge P.sid = T1.sid))) \wedge T.sid = T1.sid)\}$$

- DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge (\forall \langle A, B, C \rangle \in Parts(C \neq 'red' \vee \exists \langle P, Q, R \rangle \in Catalog(Q = A \wedge P = X)) \vee \forall \langle U, V, W \rangle \in Parts(W \neq 'green' \vee \langle M, N, L \rangle \in Catalog(N = U \wedge M = X))\}$$

■ SQL

```

SELECT C.sid
FROM   Catalog C
WHERE  (NOT EXISTS (SELECT P.pid
                    FROM   Parts P
                    WHERE  P.color = 'red' AND
                    (NOT EXISTS (SELECT C1.sid
                                FROM   Catalog C1
                                WHERE  C1.sid = C.sid AND
                                       C1.pid = P.pid))))
OR ( NOT EXISTS (SELECT P1.pid
                 FROM   Parts P1
                 WHERE  P1.color = 'green' AND
                 (NOT EXISTS (SELECT C2.sid
                             FROM   Catalog C2
                             WHERE  C2.sid = C.sid AND
                                    C2.pid = P1.pid))))
    
```

9. ■ RA

$$\rho(R1, Catalog)$$

$$\rho(R2, Catalog)$$

$$\pi_{R1.sid, R2.sid}(\sigma_{R1.pid=R2.pid \wedge R1.sid \neq R2.sid \wedge R1.cost > R2.cost}(R1 \times R2))$$

■ TRC

$$\{T \mid \exists T1 \in Catalog (\exists T2 \in Catalog$$

$$(T2.pid = T1.pid \wedge T2.sid \neq T1.sid$$

$$\wedge T2.cost < T1.cost \wedge T.sid2 = T2.sid)$$

$$\wedge T.sid1 = T1.sid)\}$$

■ DRC

$$\{\langle X, P \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists P, Q, R$$

$$(\langle P, Q, R \rangle \in Catalog \wedge Q = Y \wedge P \neq X \wedge R < Z)\}$$

■ SQL

```

SELECT C1.sid, C2.sid
FROM   Catalog C1, Catalog C2
WHERE  C1.pid = C2.pid AND C1.sid \neq C2.sid
AND    C1.cost > C2.cost
    
```

## 10. ■ RA

$$\rho(R1, Catalog)$$

$$\rho(R2, Catalog)$$

$$\pi_{R1.pid} \sigma_{R1.pid=R2.pid \wedge R1.sid \neq R2.sid} (R1 \times R2)$$

## ■ TRC

$$\{T \mid \exists T1 \in Catalog (\exists T2 \in Catalog$$

$$(T2.pid = T1.pid \wedge T2.sid \neq T1.sid$$

$$\wedge T.pid = T1.pid))\}$$

## ■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists A, B, C$$

$$\langle A, B, C \rangle \in Catalog \wedge B = Y \wedge A \neq X\}$$

## ■ SQL

```
SELECT C.pid
FROM   Catalog C
WHERE  EXISTS (SELECT C1.sid
              FROM   Catalog C1
              WHERE  C1.pid = C.pid AND C1.sid \neq C.sid )
```

## 11. ■ RA

$$\rho(R1, \pi_{sid} \sigma_{sname='YosemiteSham'} Suppliers)$$

$$\rho(R2, R1 \bowtie Catalog)$$

$$\rho(R3, R2)$$

$$\rho(R4(1 \rightarrow sid, 2 \rightarrow pid, 3 \rightarrow cost), \sigma_{R3.cost < R2.cost} (R3 \times R2))$$

$$\pi_{pid} (R2 - \pi_{sid, pid, cost} R4)$$

## ■ TRC

$$\{T \mid \exists T1 \in Catalog (\exists X \in Suppliers$$

$$(X.sname = 'YosemiteSham' \wedge X.sid = T1.sid) \wedge \neg (\exists S \in Suppliers$$

$$(S.sname = 'YosemiteSham' \wedge \exists Z \in Catalog$$

$$(Z.sid = S.sid \wedge Z.cost > T1.cost))) \wedge T.pid = T1.pid\}$$

## ■ DRC

$$\{\langle Y \rangle \mid \langle X, Y, Z \rangle \in Catalog \wedge \exists A, B, C$$

$$\langle A, B, C \rangle \in Suppliers \wedge C = 'YosemiteSham' \wedge A = X$$

$$\wedge \neg (\exists P, Q, R (\langle P, Q, R \rangle \in Suppliers \wedge R = 'YosemiteSham'$$

$$\wedge \exists I, J, K (\langle I, J, K \rangle \in Catalog (I = P \wedge K > Z))))\}$$

## ■ SQL

```

SELECT C.pid
FROM   Catalog C, Suppliers S
WHERE  S.sname = 'Yosemite Sham' AND C.sid = S.sid
      AND C.cost ≥ ALL (Select C2.cost
                       FROM   Catalog C2, Suppliers S2
                       WHERE  S2.sname = 'Yosemite Sham'
                       AND   C2.sid = S2.sid)
    
```

**Exercise 4.4** Consider the Supplier-Parts-Catalog schema from the previous question. State what the following queries compute:

1.  $\pi_{sname}(\pi_{sid}(\sigma_{color='red'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers)$
2.  $\pi_{sname}(\pi_{sid}((\sigma_{color='red'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers))$
3.  $(\pi_{sname}((\sigma_{color='red'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers)) \cap$   
 $(\pi_{sname}((\sigma_{color='green'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers))$
4.  $(\pi_{sid}((\sigma_{color='red'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers)) \cap$   
 $(\pi_{sid}((\sigma_{color='green'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers))$
5.  $\pi_{sname}((\pi_{sid,sname}((\sigma_{color='red'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers)) \cap$   
 $(\pi_{sid,sname}((\sigma_{color='green'} Parts) \bowtie (\sigma_{cost < 100} Catalog) \bowtie Suppliers)))$

**Answer 4.4** The statements can be interpreted as:

1. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars.
2. This Relational Algebra statement does not return anything because of the sequence of projection operators. Once the sid is projected, it is the only field in the set. Therefore, projecting on sname will not return anything.
3. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.
4. Find the Supplier ids of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.
5. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.