

9.3 Tuple Relational Calculus: Query Language for Relational Databases

- non-procedural/declarative language
- uses first-order predicate logic to express queries
- equivalent to relational algebra

A TRC Query is expressed as

```
{ t1.A1, t2.A2, ..., tn.An | COND(t1, t2, ..., tn, tn+1, ..., tn+m) }
```

where

- t_i, \dots, t_{n+m} are tuple variables,
- A_i is an attribute of the relation on which t_i ranges.
- COND is a formula in predicate logic involving the tuple variables t_1, \dots, t_{n+m} where t_1, \dots, t_n are the ONLY FREE VARIABLES (the remaining are BOUND by quantifiers)

The syntax for COND is defined as follows:

ATOMIC FORMULAS:

1. $R(t_i)$ is an atomic formula where R is a relation and t_i is a tuple variable.
 2. $t_i.A \text{ op } t_j.B$ is an atomic formula where op is one of $<, <=, =, <>, >, >=$
 3. $t_i.A \text{ op } c$ is an atomic formula where c is a constant
 4. $c \text{ op } t_i.A$ is an atomic formula where c is a constant
- EACH of the above atomic formulas evaluate to TRUE/FALSE

FORMULAS:

1. Each atomic formula is a formula
2. if F_1 and F_2 are formulas then so are $(F_1 \text{ and } F_2)$, $(F_1 \text{ or } F_2)$, $\text{not } (F_1)$
2. if F is a formula and t is a tuple variable then so are $(\text{Exists } t)(F)$, $(\text{Forall } t)(F)$

Query Examples: (These are the queries from problem 7.18 of the El-Masri/Navathe text).

- (1) Get names of all employees in department 5 who work more than 10 hours/week on the ProductX project.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  (Exists w) (Exists p) (works_on(w) and project(p) and
    t.ssn = w.essn and w.pno = p.pnumber and
    w.hours >= 10 and p.pname = 'ProductX') }
```

- (2) Get names of all employees who have a dependent with the same first name as themselves.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  (Exists d) (dependent(d) and t.ssn = d.essn and
    t.fname = d.dependent_name) }
```

- (3) Get the names of all employees who are directly supervised by Franklin Wong.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  (Exists e) (employee(e) and t.superssn = e.ssn and
    e.fname = 'Franklin' and e.lname = 'Wong') }
```

- (4) Get the names of all employees who work on every project.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  (Forall p) (project(p) -> (Exists w) (works_on(w) and
    w.essn = t.ssn and
    e.pno = p.pnumber)) }
```

- (5) Get the names of employees who do not work on any project.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  not (Exists w) (works_on(w) and w.essn = t.ssn) }
```

- (6) Get the names and addresses of employees who work for at least one project located in Houston but whose department does not have a location in Houston.

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  (Exists w) (Exists p) (works_on(w) and project(p) and
    t.ssn = w.essn and w.pno = p.pnumber and
    p.plocation = 'Houston') and
  not (Exists d) (dept_locations(d) and t.dno = d.dnumber and
    d.dlocation = 'Houston') }
```

- (7) Get the names and addresses of employees who work for at least one project located in Houston or whose department does not have a location in Houston. (Note: this is a slight variation of the previous query with 'but' replaced by 'or').

```
{ t.fname, t.minit, t.lname |
  employee(t) and
  ((Exists w) (Exists p) (works_on(w) and project(p) and
    t.ssn = w.essn and w.pno = p.pnumber and
    p.plocation = 'Houston') or
  not (Exists d) (dept_locations(d) and t.dno = d.dnumber and
    d.dlocation = 'Houston') ) }
```

- (8) Get the last names of all department managers who have no dependents.

```
{ t.lname | employee(t) and
  (Exists d) (department(d) and t.ssn = d.mgrssn and
    not (Exists p) (dependent(p) and
      t.ssn = p.essn)) }
```