

Logic Programming in Prolog

Part I

Basics

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Prolog Syntax

Terms

Terms represent data objects. There are 3 types of terms:

- Atoms:

- symbolic atoms begin with lower-case letter, e.g. tom, bill, a1, ...
- numeric atoms, e.g. 217, -32, 2.76, ...
- strings, e.g. "hello", "tony", ...

- Variables:

begin with upper-case letter or underscore,
e.g. X, U, _x1, Tom, A1
_ represents anonymous variable

- Structures:

- function structure: $f(t_1, \dots, t_n)$, $n \geq 0$
- list structure: $[t_1, \dots, t_n]$, $n \geq 0$

where f is a symbolic atom and t_1, \dots, t_n are terms, e.g.
edge(3,7), f(g(1),h(2,3)), f(x), ...
[a,b,c], [1,2,3,4], [f(a),X,2.76,Z,z], [[a],[b]], ...

Special notation for lists: $[H|T]$, $[X,Y|T]$, $[c_1, \dots, c_n|T]$

Prolog Syntax Continued

Relation

ordinary relation: $r(t_1, \dots, t_n)$, $n \geq 0$

where r is a symbolic atom and t_1, \dots, t_n are terms, e.g.

round, father(tom,bill), student(1111,jones,freshman,4.0), ancestor(X,Y),
groceryList(monday,[["Apples",12],["Bananas,10]]),...

built-in relation: written in infix notation usually, e.g.

$X \backslash == Y$, $X > 20$, ...

Program

consists of a finite number of facts and rules;

fact: relation.

rule: relation :- relation-1, ..., relation-n.

$n \geq 1$

e.g.

member(X,[X|_]).

member(X,[Y|T]) :- X \== Y, member(X,T).

Prolog Syntax Continued

Query

?- relation-1,...,relation-n.

used to run a program

SWI Prolog <http://www.swi-prolog.org/>

```
[raj@tinman prologCode]$ more p1.pl
sizeOfList([],0).
sizeOfList([_|T], N) :- sizeOfList(T,M), N is M+1.
```

```
[raj@tinman prologCode]$ swipl
Welcome to SWI-Prolog (Multi-threaded, 64 bits, Version 7.2.3)
Copyright (c) 1990-2015 University of Amsterdam, VU Amsterdam
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software,
and you are welcome to redistribute it under certain conditions.
Please visit http://www.swi-prolog.org for details.
```

```
For help, use ?- help(Topic). or ?- apropos(Word).
```

```
?- ['p1.pl'].
true.
```

```
?- sizeOfList([1,2,3,4,5,6],N).
N = 6.
```

```
?- halt.
[raj@tinman prologCode]$
```

Sample Programs

```
parent(a,b).  
parent(b,c).  
parent(c,d).  
parent(d,e).  
parent(c,f).
```

```
ancestor(X,Y) :- parent(X,Y).  
ancestor(X,Y) :- parent(X,Z), ancestor(Z,Y).
```

```
sibling(X,Y) :- parent(Xp,X), parent(Xp,Y), X \== Y.  
cousin(X,Y) :- parent(Xp,X), parent(Yp,Y), sibling(Xp,Yp).  
cousin(X,Y) :- parent(Xp,X), parent(Yp,Y), cousin(Xp,Yp).
```

```
grandparent(X,Y) :- parent(X,Z), parent(Z,Y).
```

List Processing in Prolog

```
append([ ],L,L).
```

```
append([A|L],Y,[A|Z]) :- append(L,Y,Z).
```

```
prefix(P,L) :- append(P,_,L).
```

```
suffix(S,L) :- append(_,S,L).
```

```
reverse([ ],[ ]).
```

```
reverse([A|L],M) :- reverse(L,L1), append(L1,[A],M).
```

```
palindrome(L) :- reverse(L,L).
```

```
min([A],A).
```

```
min([A|L],A) :- min(L,N), A < N.
```

```
min([A|L],N) :- min(L,N), A >= N.
```

```
max([A],A).
```

```
max([A|L],A) :- max(L,N), A > N.
```

```
max([A|L],N) :- max(L,N), A =< N.
```

List Processing in Prolog

Tail Recursion

```
reverse(L,R) :- reverse1(L,[],R).
```

```
reverse1([],P,P).
```

```
reverse1([X|T],P,S) :- reverse1(T,[X|P],S).
```

```
min([A],A).
```

```
min([A|T],Min) :- min1(T,A,Min).
```

```
min1([],A,A).
```

```
min1([X|T],A,Min) :- X =< A, min1(T,X,Min).
```

```
min1([X|T],A,Min) :- min1(T,A,Min).
```

similarly for max.

More Prolog Programs

```
factorial(0,1).  
factorial(N,Nfac) :-  
    N > 0,  
    M is N-1,  
    factorial(M,Mfac),  
    Nfac is N * Mfac.
```

```
odd(s(0)).  
odd(s(s(X))) :- odd(X).
```

Sorting - merge sort

```
mergesort([], []).  
mergesort([X],[X]).  
mergesort(L,M) :-  
    msplit(L,L1,L2),  
    mergesort(L1,M1),  
    mergesort(L2,M2),  
    merge(M1,M2,M).
```

```
msplit([],[],[]).  
msplit([X],[X],[]).  
msplit([X,Y|L],[X|L1],[Y|L2]) :- msplit(L,L1,L2).
```

```
merge([],L,L).  
merge(L,[],L).  
merge([X|L],[Y|M],[X|N]) :- X <= Y, merge(L,[Y|M],N).  
merge([X|L],[Y|M],[Y|N]) :- X > Y, merge([X|L],M,N).
```

Sorting - quick sort

```
quicksort([], []).
quicksort([H|T], S) :-
    qsplit(H, T, L1, L2),
    quicksort(L1, M1),
    quicksort(L2, M2),
    append(M1, [H|M2], S).
```

```
qsplit(_, [], [], []).
qsplit(H, [A|L], [A|L1], L2) :- A =< H, qsplit(H, L, L1, L2).
qsplit(H, [A|L], L1, [A|L2]) :- A > H, qsplit(H, L, L1, L2).
```

subsets, permutations

```
del(X, [X|T], T).
```

```
del(X, [Y|T], [Y|S]) :- del(X, T, S).
```

```
subset([], []).
```

```
subset(S, R) :- del(X, S, T), subset(T, R).
```

```
subset(S, [X|R]) :- del(X, S, T), subset(T, R).
```

```
permute([], []).
```

```
permute(L, [X|P]) :- del(X, L, M), permute(M, P).
```

Given two equal sized list, generate all possible pairings.

```
generate(L1, L2, Pairs) :- permute(L2, M2), combine(L1, M2, Pairs).
```

```
combine([], [], []).
```

```
combine([A|S], [B|T], [[A, B]|U]) :- combine(S, T, U).
```

Logic Puzzle

Three friends competed in a programming contest and came first, second, and third respectively. Each of them has a different first name, likes a different sport, and has a different nationality.

Write a Prolog Program to answer the questions:

Who is the Australian?

What sport did Richard play?

Some additional hints:

- Michael likes basketball and did better than the American.
- Simon, the Israeli, did better than the tennis player.
- The cricket player came first.

Logic Puzzle - continued

We will use the structure `person(Name,Nationality,Sport)` to represent the three persons and we will create a list of 3 such structures.

```
name(person(A,_,_),A).
nationality(person(_,N,_),N).
sport(person(_,_,S),S).
```

```
didBetter(A,B,[A,B,_]).
didBetter(A,C,[A,_,C]).
didBetter(B,C,[_,B,C]).
```

```
first(X,[X|_]).
```

```
makeListOfFriends(0,[]).
makeListOfFriends(N,[person(_,_,_)|L]) :-
    M is N-1,
    makeListOfFriends(M,L).
```

Logic Puzzle - continued

```
answer(Aussie, RichardSport) :-  
    makeListOfFriends(3, Friends),  
  
    didBetter(M1, M2, Friends), name(M1, michael),  
    sport(M1, basketball), nationality(M2, american),  
  
    didBetter(M3, M4, Friends), name(M3, simon),  
    nationality(M3, israeli), sport(M4, tennis),  
  
    first(M5, Friends), sport(M5, cricket),  
  
    member(Q1, Friends), name(Q1, Aussie), nationality(Q1, australian),  
  
    member(Q2, Friends), name(Q2, richard), sport(Q2, RichardSport).
```